



## Mathematical and Statistical Methods in Modeling and Conducting Pedagogical Research

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### **Abstract**

Pedagogical research relies extensively on mathematical and statistical methods to unravel the complexities of educational processes, assess the effectiveness of interventions, and inform evidence-based practices. This abstract outlines the key roles these methods play in modeling and conducting pedagogical research, emphasizing their diverse applications. The experimental design is foundational, employing randomized controlled trials and factorial designs to systematically explore the impact of various variables on educational outcomes. The meticulous collection of data through surveys, questionnaires, and observational studies allows for a comprehensive understanding of student, teacher, and institutional dynamics. Descriptive statistics, including measures of central tendency and dispersion, provide a snapshot of educational phenomena, while inferential statistics enable researchers to draw meaningful conclusions about the significance of observed patterns. Hypothesis testing and regression analysis help assess the effectiveness of teaching methods and identify factors influencing student performance. The paper underscores the critical role of mathematical and statistical methods in advancing pedagogical research. These methods not only provide rigorous analyses of educational data but also contribute to the development of evidence-based strategies that can positively impact teaching and learning practices.

**Keywords:** *Pedagogical Research; Modeling; Mathematical and Statistical Methods; Scientific Research Methods*

### **Introduction**

Since the second half of the twentieth century, in connection with the development of the information environment, the problems of global application of methods of mathematical statistics in the processing and analysis of results have intensified. Also, pedagogical research has intensified the problem of the need to apply methods of mathematical statistics in a broad sense in the practical part of activity. Accordingly, it is necessary to determine the role and significance of methods of mathematical statistics in pedagogical research, and on this basis there is a need to organize a methodology for using mathematical statistics in order to improve the level of quality and practical significance of the results. Pedagogical research, increase the requirements for pedagogical research as the main basis for expressing

the laws and principles of the pedagogical environment being studied and find methods of mathematical statistics that meet these requirements.

### ***Methods***

Analysis of the features and problems of applying methods of mathematical statistics in the process of conducting pedagogical research, determining their role and place makes it possible to develop a methodology for applying methods of mathematical statistics in pedagogical research, based on the following goals: to expand the information content of the results by identifying and confirming real trends; strengthening the visualization of the results obtained due to the representativeness of the experimental data; increasing the level of accuracy of results by proving their reproducibility. The model of the pedagogical experiment is based on a comparison of the experimental and control groups. The result of the experiment is visible in the change in the experimental group compared to the control group. This comparative experiment is used in practice in various ways. Statistical procedures were used to determine whether there were differences between the experimental and control groups. The data obtained before and after the experiment are compared or compared at the end of the experimental study. If the researcher does not have two groups, then the data before and after the experiment can be compared as usual. For example, a teacher uses a new method of teaching mathematics in 9th grade and received final results at the end of the year. By comparing the results obtained with the results of previous years, it creates an overall comparison, that is, changes.

### ***Discussion***

Experimental work is an integral part of scientific and pedagogical research and is the main criterion for confirming the reliability, practical significance and applicability of the results of any research in this field.

Teacher-researchers and practicing teachers strive to improve their pedagogical and methodological position, find confirmation of applied pedagogical innovations, and implement qualitative changes in education through experimental work dedicated to solving specific educational problems. Therefore, there may be different reasons and motives for researchers and teaching practitioners in organizing and participating in experimental work, but there is only one condition, according to which each leader who decides to contribute to this process must be a master of his profession, use all his professional skills. To achieve high results during an experiment, a researcher must be able to plan his work, clearly define a system of tasks, highlight important ones among them, be able to find ways to quickly and economically complete assigned tasks, implement quick and accurate control over the completion of tasks, be able to make changes and adjustments related to organization of work, be able to analyze the overall results obtained, compare them with established requirements, have a system of special knowledge and skills related to identifying the reasons for non-fulfillment of requirements and the ability to eliminate them.

Systematically implemented experimental work in the context of educational reform shows that careful development of experimental programs, content and methodological tools used, and correct determination of the scope of implementation is the key to achieving the goals and is considered as one of the conditions.

There are a number of objective and subjective factors that influence the quality of experimental work. In particular, among the subjective factors we can note the wishes of the researcher conducting the experiment, his level of ambition, and among the objective factors - the legal, pedagogical and psychological requirements for experimental work.

These requirements include:

1. Type of experimental work (research, confirmatory and formative), scale (at the level of the republic, region, region, city and district, interschool, school level, individual and collective experimental field); It can be expressed in the scale of experimental work (covering a number of subjects, a quarter, an academic year, several years depending on the duration, volume of educational material) and others.
2. The administration of an educational institution should implement a set of measures related to ensuring the successful implementation of tasks related to the organization of experimental work, including: developing motivational conditions for attracting practicing teachers to the process of experimental testing; identify legal and regulatory grounds aimed at protecting all participants in the legal process (teachers, students, their parents) from possible negative consequences; It is necessary to achieve certain requirements for the participants in the experiment.

All stages of experimental work should be aimed at ensuring the fulfillment of the following requirements, which involve the implementation of clearly defined goals and objectives:

1. Initially, the development of a program of experimental work that allows you to manage pedagogical processes and the necessary amendments to it; it should reflect the plan of activities associated with the experiment, the expected results and methods for determining the level of achievement.
2. Analyzes should be carried out based on the results of a certain period of experimental work and presented in the form of reports, certificates and articles. This is not an unnecessary formality, but a necessary condition for experimental work, the reliability of experimental results, and a factor that determines the significance of the event being implemented. Without clarifying the issues in this regard, it remains abstract what the researcher who conducted the experiment decided, what results he expected and based on what evaluation criteria, what was achieved as a result.

The pre-experimental stage is an in-depth theorizing of previously published work on the topic; identify unresolved problems; selection of the subject of this study; setting the goal and objectives of the study; study the real practice of solving this problem; studying the measures available in theory and practice to help solve the problem; includes a statement of the research hypothesis. He has to experimentally prove novelty, unusualness, contrary to existing ideas. The difference between the observed results and the theoretically expected result may vary. As a result of statistical evaluation of this as evidence, a particular hypothesis can be accepted with a certain probability, that is, if this difference is large, the hypothesis is not accepted, otherwise it is accepted. The branch of mathematical statistics that deals with this problem is called the theory of statistical hypotheses. A statistical hypothesis is a hypothesis about a random variable or phenomenon that we want to test based on the available data. Examples of statistical hypotheses in educational research:

**Hypothesis 1:** Student learning is stochastically (probably) dependent on their level of knowledge.

**Hypothesis 2.** There is no significant difference in performance in the elementary mathematics course among students who entered school at 6 or 7 years old.

The null hypothesis is the main hypothesis being tested, which is formed as the absence of a difference, the absence of factor influence, the absence of an effect, the value of a sample characteristic equal to zero, etc.

An example of a null hypothesis in pedagogy is the statement that the difference in test results obtained in two groups is due to random reasons. The other hypothesis being tested is called the competing or alternative hypothesis. For example, an alternative to the above-mentioned hypothesis  $H_0$  is hypothesis  $H_1$ : the level of work performed in both groups of students is different, and this difference is

determined by the influence of non-random factors, one or another teaching method. A pre-established hypothesis may be true or false, so it needs to be tested. If such a survey is carried out using statistical methods, it is called a statistical survey. The next task of statistical analysis is the joint analysis of several samples, which is solved after determining the main characteristics of the sample and analyzing one sample. An important question that arises when analyzing two samples is whether there is a difference between the samples. This is usually done by checking the statistical analysis to ensure that they are not drawn from the same association or that the means are equal. If the shape of the distribution or the distribution function of the sample is given, then the problem of estimating the difference between two groups of independent observations is solved using parametric statistical tests: if the comparison of samples is carried out by means ( $X$  and  $U$ ), Student's test ( $t$ ) or Fisher's test ( $F$ ), if samples are compared by their variance. Using parametric statistical criteria without first checking the appearance of the distribution can lead to unexpected errors in the process of testing the working hypothesis. To overcome the difficulties manifested in the practice of pedagogical research, it is necessary to use nonparametric statistical criteria. These are the sign test, Wicoxon binomial test, Van der Waerden test and Spearman test. Their choice depends on certain conditions, although it does not require a large amount of knowledge and choice, or an idea of distribution. Nonparametric statistical tests are based on the assumption that the sample distribution is free and the observations are independent. The group of parametric criteria of mathematical statistics methods includes methods for calculating statistical expressions, constructing graphs of normality of distributions, and testing the hypothesis that two samples belong to the same association. These methods are based on the assumption that the sampling distribution follows a normal (Gaussian) distribution.

## **Conclusion**

Based on the above, we can say that mathematical and statistical methods play a crucial role in modeling and conducting pedagogical research. These methods help researchers analyze data, draw meaningful conclusions, and make informed decisions in the field of education. We can discuss about some key ways in which mathematical and statistical methods are applied in pedagogical research:

### **1. Experimental Design**

**Randomized Controlled Trials (RCTs):** Random assignment of participants to different groups helps ensure that any observed effects are likely due to the treatment or intervention.

**Factorial Designs:** Examining the effects of multiple variables simultaneously to understand their individual and interactive impacts on educational outcomes.

### **2. Data Collection**

**Surveys and Questionnaires:** Designing effective survey instruments and analyzing the collected responses to gain insights into student, teacher, or institutional characteristics.

**Observational Studies:** Systematically observing and recording behaviors or events in educational settings, and using statistical methods to analyze patterns.

### **3. Descriptive Statistics**

**Measures of Central Tendency:** Calculating mean, median, and mode to describe the average or typical performance of students or groups.

**Measures of Dispersion:** Assessing the spread or variability of data using metrics like standard deviation.

#### 4. Inferential Statistics

**Hypothesis Testing:** Assessing whether observed differences or relationships in data are statistically significant or if they could have occurred by chance.

**Regression Analysis:** Examining the relationship between variables, such as the impact of teaching methods on student performance.

#### 5. Modeling and Simulation

**Educational Models:** Developing mathematical models to represent educational systems, learning processes, or student progress over time.

**Monte Carlo Simulations:** Using simulation techniques to model complex educational scenarios and assess the potential outcomes of various interventions.

#### 6. Longitudinal Data Analysis

**Tracking Student Progress Over Time:** Analyzing data collected at multiple points to understand the trajectory of student learning and identify factors influencing educational development.

#### 7. Meta-Analysis

**Synthesizing Research Findings:** Combining results from multiple studies to provide a more comprehensive and robust understanding of the effectiveness of educational interventions.

#### 8. Predictive Analytics

**Machine Learning Algorithms:** Applying advanced statistical methods to predict educational outcomes, identify patterns, and personalize learning experiences.

#### 9. Ethical Considerations

**Fairness and Bias Analysis:** Ensuring that statistical analyses are conducted ethically, and addressing issues related to fairness and bias in educational research.

#### 10. Interdisciplinary Research

**Collaboration with Educational Psychologists and Sociologists:** Combining mathematical and statistical methods with insights from psychology and sociology to create a holistic understanding of educational phenomena.

In summary, the integration of mathematical and statistical methods in pedagogical research enhances the rigor and validity of studies, providing valuable insights that can inform educational policies, practices, and interventions. It's essential for researchers and educators to collaborate across disciplines to leverage the full potential of these methods in improving educational outcomes.

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